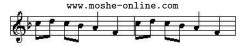
How do you recognize a Voodoo decision theory?

Info-Gap

Moshe Sniedovich

Department of Mathematics and Statistics The University of Melbourne



School of Mathematical and Geospatial Sciences RMIT June 26, 2009

Voodoo decision theories have a number of major advantages over scientific theories. It is not surprising therefore that they can become very popular in scientific circles, including refereed journals. For this and other reasons it is very important and useful to acquire basic skills to identify such theories. In this presentation I provide some practical tips for the identification of Voodoo decision theories, especially theories that are designed for robust decision-making in the face of severe uncertainty. I illustrate these tips in action by a formal,

Info-Gap

decision-making.moshe-online.com

rigorous, mathematical analysis of Info-Gap decision theory.

Program

Info-Gap

- How do you make robust decisions in the face of severe uncertainty?
 - Severe Uncertainty
 - Voodoo Decision Theories
 - Info-Gap Decision Theory
 - Classical Decision Theory
 - Australian perspective
 - My Info-Gap Campaign
- Collaboration
- Site visit: decision-making.moshe-online.com
- FAQs

This is a

Math Classification

presentation.

Math Classification MA + 18

versions can be found at

decision-making.moshe-online.com

Severe Uncertainty

Working Assumption

|Estimate - True Value| >>>
$$\varepsilon$$
 > 0

The estimate we have is

- A wild guess.
- A poor indication of the true value.
- Likely to be substantially wrong.

Difficulty

Results obtained in the neighborhood of the estimate are likely to be substantially wrong in the neighborhood of the true value.

Severe uncertainty

Region of Severe Uncertainty true value poor estimate

Uncertainty Models for Severe Uncertainty

- Non-probabilistic
- Likelihood-free

AU Perspective

What is the most popular methodology for robust decision-making under severe uncertainty in a number of prestigious research organizations in Australia



Decision-Making Under Severe Uncertainty



bio-security

homeland-security

AU 000000

A new reliable technical indicator for predicting financial markets



AU

000000

Planning for robust reserve networks using uncertainty analysis

... In summary, we recommend info-gap uncertainty analysis as a standard practice in computational reserve planning. The need for robust reserve plans may change the way biological data are interpreted. It also may change the way reserve selection results are evaluated, interpreted and communicated. Information-gap decision theory provides a standardized methodological framework in which implementing reserve selection uncertainty analyses is relatively straightforward. We believe that alternative planning methods that consider robustness to model and data error should be preferred whenever models are based on uncertain data, which is probably the case with nearly all data sets used in reserve planning . . .

> Ecological Modelling, 199, pp. 115-124, 2006 Finland (1), USA (3), Australia (3), Israel (2)

αεδα

Applied Environmental Decision Analysis

A Commonwealth Environment Research Facility smart science for wise decisions

SEARCH



AII

000000





About AEDA

Core Researchers

Research Themes

News

Events

Contact Us

Site Map

Events & Workshops

Home » Events & Workshops

E Print version

More Information → Info-Gap Course

UP & COMING ...

15 - 19 Sept, 2008	Info-Gap Applications in Ecological Decision Making (5 Day workshop with Prof. Yakov Ben-Haim).		
	6 - 10 Oct, 2008	Multispecies Management Workshop, Brisbane, Queensland	

AU Perspective

AU

000000

New Secret Weapon Against Severe Uncertainty

$$\hat{\alpha}(q) := \max\{\alpha \geq 0 : r \leq R(q, u), \forall u \in U(\alpha, \tilde{u})\}, q \in \mathcal{Q}$$

Known as

Info-Gap Robustness Model

Ben-Haim (1996, 2001, 2006)

Very popular in a number of research organizations in Australia





Encarta online Encyclopedia

Voodoo n

- A religion practiced throughout Caribbean countries, especially Haiti, that is a combination of Roman Catholic rituals and animistic beliefs of Dahomean enslaved laborers, involving magic communication with ancestors.
- Somebody who practices voodoo.
- A charm, spell, or fetish regarded by those who practice voodoo as having magical powers.
- A belief, theory, or method that lacks sufficient evidence or proof.









Good Company

- Voodoo economics
- Voodoo science
- Voodoo mathematics
- Voodoo Decision-making

Apparently very popular,

Example

The behavior of Kropotkin's cooperators is something like that of decision makers using Jeffrey expected utility model in the Max and Moritz situation. Are ground squirrels and vampires using voodoo decision theory?

> Brian Skyrms Evolution of the Social Contract Cambridge University Press, 1996.

Issue:

Evidential dependence, but causal independence.

Voodoo Decision-Making vs Scientific decision-making

Major Obstacles to Progress in Scientific Decision-Making

Info-Gap

- Garbage In Garbage Out
- The results of an analysis can be only as good as the estimates on which it is based.
- Beware of the distinction between local and global analysis.
- Thou shalt not contradict thyself!

They do not hinder progress in Voodoo Decision-making!

Example: The legend

An old legend has it that an ancient treasure is hidden in an Asian-Pacific island.

Info-Gap



You are in charge of the treasure hunt. How would you plan the operation?

The legend

Main issue: location, location, location!

Terminology



The Fundamental Theorem of Voodoo Decision Making



Severe Uncertainty

1.2.3 Recipe

- Ignore the severity of the uncertainty.
- 2 Focus on the substantially wrong estimate you have.
- Conduct the analysis in the immediate neighborhood of this estimate.

Voodoo Decision-Making

Region of Severe Uncertainty poor estimate



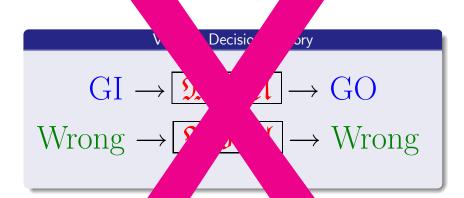


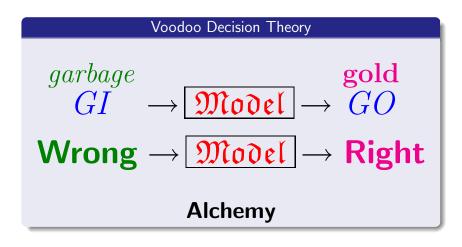
$$GI \to \boxed{\mathfrak{Model}} \to GO$$

$$Wrong \to \boxed{\mathfrak{Model}} \to Wrong$$

The robustness of any decision and the risk incurred in making that decision is only as good as the estimates on which it is based. Making estimation even more challenging, virtually all estimates that affect decisions are uncertain. Uncertainty can not be eliminated, but it can be managed.

Top Ten Challenges for Making Robust Decisions The Decision Expert Newsletter, Volume 1; Issue 2 http://www.robustdecisions.com/newsletter0102.php





Question

What is the most popular Voodoo Decision Theory for robust decision-making under severe uncertainty in a number of research centers in

Info-Gap

Australia



A new reliable technical indicator for predicting financial markets



Applied ecology and conservation biology



This seminar

Objective of this seminar

- Overview of Voodoo Decision-Making (5000 BC)
- Tips for identifying Voodoo Decision Theories
- Overview of Info-Gap Decision Theory (1996)
- Progress report on my Info-Gap Campaign (2006 –)
- Raise/Answer questions



The Spin Stops Here!

This seminar

Why bother about Voodoo Decision Theories?

- Party
- Refereeing
- Reviewing research proposals
- Examining PhD Theses
- Assessing financial investment strategies
- Medical equipment/treatment
- Evaluating your very own models and theories

This seminar

Tips for recognizing Voodoo Decision Theories

Info-Gap

- Clear the fog, spin, rhetoric
- Check the assumptions
- Ask yourself: isn't it too good to be true?
- Check the GIGO Axiom
- Double-check: are we reinventing the (square) wheel?
- Apply your mathematical skills!
- Check the 10 Natural Laws of Operations Analysis
- Consult books such as Fashionable Nonsense: Postmodern Intellectuals' Abuse of Science (Alan Sokal, Jean Bricmont, 1999) Voodoo Science: The Road from Foolishness to Fraud (Robert Park, 2001)











Info-Gap Revisited

Impressive Self-Portrait

Info-Gap

Info-gap decision theory is radically different from all current theories of decision under uncertainty. The difference originates in the modelling of uncertainty as an information gap rather than as a probability. The need for info-gap modeling and management of uncertainty arises in dealing with severe lack of information and highly unstructured uncertainty. Ben-Haim [2006, p. xii]

In this book we concentrate on the fairly new concept of information-gap uncertainty, whose differences from more classical approaches to uncertainty are real and deep. Ben-Haim [2006, p. 11]

Info-Gap

Obvious Questions

Info-Gap

000000000000000000

- Does Info-Gap substantiate these very strong claims?
- Are these claims valid?

Not So Obvious Answers

- No. it does not.
- Certainly not.

It is therefore important to subject Info-Gap to a formal analysis – that actually should have been done seven years ago:

Info-Gap **Formal** Analysis VS Classical Decision Theory

Good news: should take no more than 5-10 minutes!

Complete Generic Robustness Model

Info-Gap

00000000000000000

$$\hat{\alpha}(r_c) := \max_{q \in \mathbb{Q}} \max \{ \alpha \ge 0 : r_c \le R(q, u), \forall u \in \mathcal{U}(\alpha, \tilde{u}) \}$$

$$\mathcal{U}(\alpha, \tilde{u}) \subseteq \mathcal{U}(\alpha + \varepsilon, \tilde{u}), \forall \varepsilon > 0$$

Region of Severe Uncertainty, U

 $\mathfrak{U} = \text{total region of uncertainty}$

Complete Generic Robustness Model

$$\hat{\alpha}(r_c) := \max_{q \in \mathbb{Q}} \max \{ \alpha \ge 0 : r_c \le R(q, u), \forall u \in \mathcal{U}(\alpha, \tilde{u}) \}$$

Fundamental FAQs

Is this new?
 Definitely not!

2 Is this radically different? Definitely not!

Does it make sense?

Definitely not!

So what is all this hype about Info-Gap ?!

Good question!

First Impression

Info-Gap

0000000000000000

Complete Generic Robustness Model

$$\hat{\alpha}(r_c) := \max_{q \in \mathbb{Q}} \max \{ \alpha \ge 0 : r_c \le R(q, u) \forall u \in \mathcal{U}(\alpha, \tilde{u}) \}$$

Observations

- This model does not deal with severe uncertainty, it simply and unceremoniously ignores it.
- The analysis is invariant with \mathfrak{U} : the same solution for all \mathfrak{U} such that $\mathcal{U}(\hat{\alpha}(r_c), \tilde{u}) \subseteq \mathfrak{U}$.
- This model is fundamentally flawed.
- This model advocates Voodoo decision-making.

First Impression

Info-Gap

00000000000000000

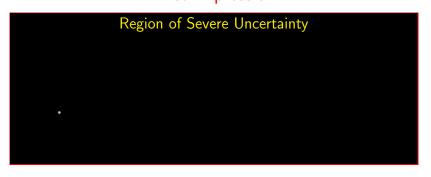
Fool-Proof Recipe

- Step 1: *Ignore* the severe uncertainty.
- Step 2: Focus instead on the poor estimate and its immediate neighborhood.

Region of Severe Uncertainty



First Impression





Recall that this is voodoo decision making!

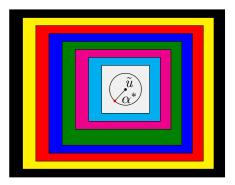
Complete Generic Robustness Model

Info-Gap

00000000000000000

 $\alpha^* := \max_{q \in \mathbb{Q}} \max \{ \alpha \ge 0 : r_c \le R(q, u), \forall u \in \mathcal{U}(\alpha, \tilde{u}) \}$

Fundamental Flaw



More formally

Invariance Theorem (Sniedovich, 2007)

Info-Gap

Info-Gap's robustness model is invariant to the size of the total region of uncertainty $\mathfrak U$ for all $\mathfrak U$ larger than $\mathcal U(\alpha^*, \tilde u)$, where $\alpha^* := \hat{\alpha}(r_c)$.

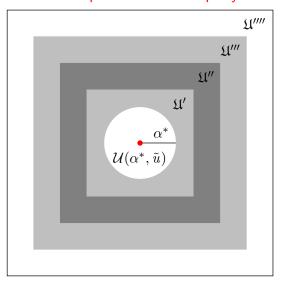
That is, the model yields the same results for all $\mathfrak U$ such that

$$\mathcal{U}(\alpha^* + \varepsilon, \tilde{u}) \subseteq \mathfrak{U}, \ \varepsilon > o$$

Info-Gap's Invariance Property

Info-Gap

00000000000000000



Maximin Theorem (Sniedovich 2007, 2008)

Info-Gap's robustness model is a simple instance of Wald's Maximin model (circa 1940). Specifically,

$$\alpha(q) := \max_{\alpha \ge 0} \left\{ \alpha : r_c \le R(q, u), \forall u \in \mathcal{U}(\alpha, \tilde{u}) \right\}, \ q \in \mathbb{Q}$$
$$= \max_{\alpha \ge 0} \min_{u \in \mathcal{U}(\alpha, \tilde{u})} \psi(q, \alpha, u)$$

Info-Gap

where

$$\psi(q, \alpha, u) := \begin{cases} \alpha, & r_c \le R(q, u) \\ 0, & r_c > R(q, u) \end{cases}, \alpha \ge 0, q \in \mathbb{Q}, u \in \mathcal{U}(\alpha, \tilde{u})$$

Info-Gap: Typical misconception

Treasure Hunt



Myth:

0000000000000000000

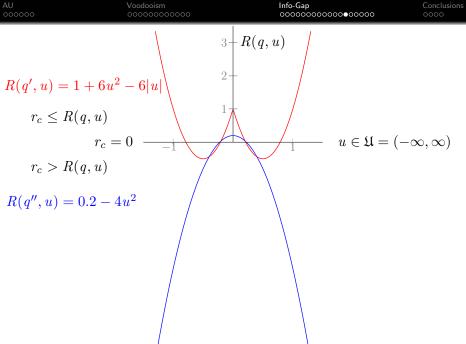
Info-Gap

How wrong can I be, yet be safe?

- Region of uncertainty.
- Estimate of the location.
- Region affecting Info-Gap's analysis.
- True (unknown) location.

Fact:

Info-gap may conduct its robustness analysis in the vicinity of Brisbane (QLD), whereas for all we know the true location of the treasure may be somewhere in the middle of the Simpson desert or perhaps in down town Melbourne (VIC). Perhaps.



Local vs Global Robustness



"Yellow" Device Very powerful. Covers most of the screen.



"Green" Device. Very weak. Effective only in the middle of the screen.

The Winner!!!! (a la Info-Gap)

Quiz on Info-Gap:

Recognizing Voodoo Decision Theories

- Fog, spin, rhetoric
- Assumptions
- Too good to be true!
- Violation of the GIGO Axiom
- Reinvention of a square wheel
- Local vs Global
- Contradiction
- 10 Natural Laws of Operations Analysis

Bottom Line

Fool-Proof Recipe

Step 1: *Ignore* the severe uncertainty.

Step 2: Focus instead on the poor estimate and its immediate neighborhood.

Region of Severe Uncertainty

Neighborhood of a Wild guess

True value



Local Maximin Analysis

Australian Perspective



Info-Gap

00000000000000000

Why am I here?

Issues

Info-Gap

00000000000000000

- Refereed Publications
- Research Grants
- PhD Theses
- Keynote Lectures
- Workshops

Voodoo decision theories are not good for

- Decision-Making
- Mathematics
- Science
- Australia

Conclusions

- Decision-making under severe uncertainty is difficult.
- It is a thriving area of research/practice.
- The Robust Optimization literature is extremely relevant.
- The Decision Theory literature is extremely relevant.
- The Operations Research literature is very relevant.
- Beware of Voodoo decision theories.
- Info-Gap decision theory is a Voodoo decision theory.
- Info-Gap decision theory is a square wheel.

Join my campaign!



The Ten Natural Laws of Operations Analysis

- Ignore the problem and go immediately to the solution, that is where the profit lies.
- There are no small problems only small budgets.
- Names are control variables.
- Clarity of presentation leads to aptness of critique.
- Invention of the wheel is always on the direct path of a cost plus contract.
- Undesirable results stem only from bad analysis.
- It is better to extend an error than to admit to a mistake.
- Progress is a function of the assumed reference system.
- Rigorous solutions to assumed problems are easier to sell than assumed solutions to rigorous problems.
- In desperation address the problem.

Bob Bedow, *Interfaces* 7(3), p. 122, 1979.



- Voodoo Decision-Making
- Responsible Decisions
- Severe Uncertainty
- Maximin
- Info-Gap Decision Theory
- Satisficing vs Optimizing

- Too Good to be True!
- Reinventing a Square Wheel
- Black Swans
- New Nostradamuses
- Alchemy
- The Spin Stops Here!



Bibliography

- Ben-Haim, Y. 1996. Robust Reliability in the Mechanical Science, Springer Verlag.
- Ben-Haim, Y. (1999). Design certification with information-gap uncertainty, Structural Safety, 2, 269-289.
- Ben-Haim, Y. 2001. Information Gap Decision Theory. Academic Press.
- Ben-Haim, Y. 2006. Info-Gap Decision Theory. Elsevier.
- Ben-Haim, Y. 2008. Info-Gap Forecasting and the Advantage of Sub-Optimal Models, European Journal of Operational Research, in press.
- Ben-Tal A. & Nemirovski, A. 1999. Robust solutions of uncertain linear programs, OR Letters, 25, 1-13.

Ben-Tal A. & Nemirovski, A. 2002. Robust optimization – methodology and applications, Mathematical Programming, Ser. B, 92, 453?480.

- Ben-Tal A. El Ghaoui, L. & Nemirovski, A. 2006. Mathematical Programming, Special issue on Robust Optimization, 107(1-2).
- Cagetti, M., Hansen, L.P., Sargent, T., and Williams, N. 2002. Robustness and Pricing with Uncertain Growth, The Review of Financial Studies, 15, 2, 363-404.
- Davidovitch, L. and Ben-Haim, Y. 2008. *Profiling for* crime reduction under severely uncertain elasticities, working paper www.technion.ac.il/ yakov/IGT/lior15prof.pdf.
- Dembo, R.S. 1991. Scenario optimization. Annals of Operations Research 30(1): 63-80.

- Demyanov, V.M. and Malozemov, V.N. 1990. Introduction to Minimax. Dover.
- Du, D.Z. and Pardalos, P.M. 1995. Minimax and Applications, Springer Verlag.
- Eiselt, H.A., Sandblom, C.L. and Jain, N. 1998. A Spatial Criterion as Decision Aid for Capital Projects: Locating a Sewage Treatment Plant in Halifax, Nova Scotia, Journal of the Operational Research Society, 49(1), 23-27.
- Eiselt, H.A. and Langley A. 1990. Some extensions of domain criteria in decision making under uncertainty, Decision Sciences, 21, 138-153.
- Francis, R.L., McGinnis, Jr, L.F. & White, J.A. 1992. Facility Layout and Location: An Analytical Approach. Prentice Hall.



- Hall, J. & Ben-Haim, Y. 2007. Making Responsible Decisions (When it Seems that You Can't). www.floodrisknet.org.uk/a/2007/11/hall -benhaim.pdf.
- Huber, P.J. 1981. Robust Statistics. Wiley, New York.
- Kouvelis, P. & Yu, G. 1997. Robust Discrete Optimization and Its Applications., Kluwer.
- Rawls, J. (2005). *Theory of Justice*, Belknap Press, Cambridge, MA.
- Reemstem, R. and Rückmann, J. (1998). Semi-Infinite Programming, Kluwer, Boston.
- Resnik, M.D. 1987. *Choices: an Introduction to Decision Theory.* University of Minnesota Press: Minneapolis.

Rosenhead M.J, Elton M, Gupta S.K. 1972. Robustness and Optimality as Criteria for Strategic Decisions, *Operational Research Quarterly*, 23(4), 413-430.

- Rustem, B. & Howe, M. 2002. *Algorithms for Worst-case Design and Applications to Risk Management*. Princeton University Press.
- Schneller G.O. and Sphicas, G.P. (1983). Decision making under uncertainty: Starr's Domain criterion, Theory and Decision. 15. 321-336.
- Skyrms, B. 1996. *Evolution of the Social Contract,* Cambridge University Press.
- Sniedovich, M. 2007. The art and science of modeling decision-making under severe uncertainty. *Journal of Manufacturing and Services*, 1(1-2): 111-136.

Sniedovich, M. 2008. Wald's Maximin Model: A Treasure in Disguise! Journal of Risk Finance, 9(3), 287-291.

- A. L. Soyster, A.L. 1973. Convex Programming with Set-Inclusive Constraints and Applications to Inexact Linear Programming, it Operations Research, 21(5), 1154-1157.
- Starr, M.K. 1962. Product design and decision theory, Prentice-Hall, Englewood Cliffs, NJ.
- Starr, M. K. 1966. A Discussion of Some Normative Criteria for Decision-Making Under Uncertainty, Industrial Management Review, 8(1), 71-78.
- Tintner, G. 1952. Abraham Wald's contributions to econometrics. The Annals of Mathematical Statistics 23(1): 21-28.

Vladimirou, H. & Zenios, S.A. 1997. Stochastic Programming and Robust Optimization. In Gal, T, & Greenberg H.J. (ed.), Advances in Sensitivity Analysis and Parametric Programming. Kluwer.

- von Neumann, J. 1928. Zur theories der gesellschaftsspiele, Math. Annalen, Volume 100, 295-320.
- von Neumann, J. and Morgenstern, O. 1944. Theory of Games and Economic Behavior, Princeton University Press.
- Wald, A. 1945. Statistical decision functions which minimize the maximum risk, The Annals of Mathematics, 46(2), 265-280.
- Wald, A. 1950. Statistical Decision Functions. John Wiley.