AU 00000 RO 0000 Voodooism 0000000000 Info-Gap Conclusions

Black Swans, Modern Nostradamuses, Voodoo Decision Theories, Info-Gaps, and the Science of Decision-Making in the Face of Severe Uncertainty

Moshe Sniedovich



Decision Theory	RO	Voodooism
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Program

- How do you make robust decisions in the face of severe uncertainty?
 - Black Swans
 - Modern Nostradamuses
 - Voodoo Decision Theories
 - Info-Gap Decision Theory
 - Classical Decision Theory
 - Australian perspective
 - My Info-Gap Campaign
- Collaboration
- Site visit: decision-making.moshe-online.com
- FAQs



AU Perspective

Decision Theory

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What is the most popular methodology for robust decision-making under severe uncertainty in a number of research centers in Australia



AU Perspective: Example

Decision Theory

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Planning for robust reserve networks using uncertainty analysis

Voodooism

... In summary, we recommend info-gap uncertainty analysis as a standard practice in computational reserve planning. The need for robust reserve plans may change the way biological data are interpreted. It also may change the way reserve selection results are evaluated, interpreted and communicated. Information-gap decision theory provides a standardized methodological framework in which implementing reserve selection uncertainty analyses is relatively straightforward. We believe that alternative planning methods that consider robustness to model and data error should be preferred whenever models are based on uncertain data, which is probably the case with nearly all data sets used in reserve planning . . .

> Ecological Modelling, 199, pp. 115-124, 2006 Authors: Finland (1), USA (3), Australia (3), Israel (2)

Conclusions

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More Information → Info-Gap Course

UP & COMING ...

15 - 19 Sept, 2008	Info-Gap Applications in Ecological Decision Making (5 Day worksh	op with Prof. Yakov Ben-Haim).
6 - 10 Oct, 2008	Multispecies Management Workshop, Brisbane, Queensland	1000
		6/67

New Secret Weapon Against Severe Uncertainty

 $\hat{\alpha}(q) := \max\{\alpha \ge 0 : r \le R(q, u), \forall u \in U(\alpha, \tilde{u})\}, q \in \mathcal{Q}$

Known as

Info-Gap Robustness Model Ben-Haim (1996, 2001, 2006)

Very popular in a number of research centers in Australia



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This seminar							

Objective of this seminar

- Overview of classical decision theory (1940-50)
- Overview of Robust Decision-Making (1960s)
- Overview of Voodoo Decision-Making (5000 BC)
- Overview of Info-Gap Decision Theory (1996)
- Progress report on my Info-Gap Campaign (2006 -)
- Raise/Answer questions



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Classical Decision Theory



Eg.

620-262: Decision Making

Good morning Sir/Madam:

I left on your doorstep four envelopes. Each contains a sum of money. You are welcome to open any one of these envelopes and keep the money you find there.

Please note that as soon as you open an envelope, the other three will automatically self-destruct, so think carefully about which of these envelopes you should open.

To help you decide what you should do, I printed on each envelope the possible values of the amount of money (in Australian dollars) you may find in it. The amount that is actually there is equal to one of these figures.

Unfortunately the entire project is under severe uncertainty so I cannot tell you more than this.

Good luck!

Joe.

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So	What Do Y	'ou do?				
	Example					
	Envelope	Pos	sible An	nount (Austra	lian dollars)	
	E1		2	0, 10, 300, 78	6	
	E2	2,40000,	102349,	5000000,999	999999, 5643543	32
	E3			201, 202		
	E4			200		

Vote!

- What is a decision problem ?
- How do we model a decision problem?
- How do we solve a decision problem?

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Decision	Tables				

Think about your problem as a table, where

- rows represents decisions
- columns represent the relevant possible states of nature
- entries represent the associated payoffs/rewards/costs

Exa	mple						
-	Env Possible Amount (\$AU)						
-	E1	20	10	300	786		
	E2	2	4000000	102349	500000000	56435432	
	E3	201	202				
	E4	200					

Classification of Uncertainty

Decision Theory

Classical decision theory distinguishes between three levels of uncertainty regarding the state of nature, namely

Voodooism

Info-Gap

- Certainty
- Risk
- Strict Uncertainty

Terminology:

Strict Uncertainty \equiv Severe Uncertainty

- \equiv Ignorance
- \equiv True Uncertainty
- \equiv Knightian Uncertainty
- $\equiv \mathsf{Deep}$
- $\equiv \mathsf{Extreme}$
- $\equiv \mathsf{Hard}$
- \equiv Fundamental

Conclusions



Classical decision theory offers two basic principles for dealing with severe uncertainty, namely

- Laplace's Principle (1825)
- Wald's Principle (1940)

Conceptually:



AU Decision Theory RO Voodooism Info-Gap Conclusions

Laplace's Principle of Insufficient Reason (1825)

By symmentry: Assume that all the states are equally likely, thus use a uniform distribution function (μ) on the state space and regard the problem as decision-making under risk.

Laplace's Decision Rule

$$\max_{d \in \mathbb{D}} \int_{s \in S(d)} r(s, d) \mu(s) ds \qquad \text{Continuous case}$$
$$\max_{d \in \mathbb{D}} \frac{1}{|S(d)|} \sum_{s \in S(d)} r(s, d) \qquad \text{Discrete case}$$

Inspired by Von Neumann's [1928] Maximin model for 0-sum, 2-person games: Mother Nature is and adversary and is playing against you, hence apply the worst-case scenario. This transforms the problem into a decision-making under certainty.

Nice Plain Language Formulation

The maximin rule tells us to rank alternatives by their worst possible outcomes: we are to adopt the alternative the worst outcome of which is superior to the worst outcome of the others.

Rawls, J., Theory of Justice, 1971, p. 152

Wald's Maximin Principle (1940)

Historical perspective

The gods to-day stand friendly, that we may, Lovers of peace, lead on our days to age! But, since the affairs of men rests still incertain, Let's reason with the worst that may befall. William Shakespeare (1564-1616) Julius Caesar, Act 5, Scene 1

Classic Format					
You!	Mama				
max	min	$f(\mathbf{d}, \mathbf{s})$			
$d{\in}\mathbb{D}$	$s \in S(d)$				

About Maximin/Minimax formulations

Classical Format					
	$\max_{d\in\mathbb{D}}$	$\min_{\substack{s \in S(d)}}$	f(d,s)		

Mathematical Programming Format

$$\begin{array}{c} \underset{d \in \mathbb{D} \\ v \in \mathbb{R} \end{array}}{\text{You!}} \left\{ v : f(d,s) \geq v \ , \ \forall s \in S(d) \right\} \end{array}$$

Note: if S(d) is "continuous", then this is a semi-infinite program.

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Example							
	Env	Dnv Possible Amount (\$AU)					
	E1	20	10	300	786		
	E2	2	4000	102349	50000	56435	
	E3	201	202				
	E4	200					

Example

Env		Possik	ole Amoi	Laplace	Wald		
E1	20	10	300	786		279	10
E2	2	4000	10234	50000	56435	24134.2	2
E3	201	202				201.5	201
E4	200					200	200

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Laplace	vs Wald				

Example

Env		Possil	ole Amoi	Laplace	Wald		
E1	20	10	300	786		279	10
E2	2	4000	10234	50000	56435	24134.2	2
E3	201	202				201.5	201
E4	200					200	200

WIKIPEDIA

Robustness is the quality of being able to withstand stresses, pressures, or changes in procedure or circumstance. A system, organism or design may be said to be "robust" if it is capable of coping well with variations (sometimes unpredictable variations) in its operating environment with minimal damage, alteration or loss of functionality.

- Applies to both (known) variability and uncertainty
- Origin: probably late 1920's (game theory).
- In OR and Optimization: late 1960s early 1970s.
- Major difficulty: solution procedures.
- A very "hot" area of research these days ...
- See bibliography



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[1, 8]

[1, 2]

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Robust Decision-Making

Role of Maximin/Minimax in Robustness Analysis

But as we defined robustness to mean insensitivity with regard to small deviations from assumptions, any quantitative measure of robustness must somehow be concerned with the maximum degradation of performance possible for an ϵ -deviation from the assumptions. The optimally robust procedure minimizes this degradation and hence will be a minimax procedure of some kind.

Huber (1981, pp. 16-17)

Experience: Modeling aspects can be subtle!

- Optimizing vs Satisficing
- Complete vs Partial vs Local
- (Mis) Interpretation

Classification

- Robust Satisficing (eg. Soyster (1973), Ben-Tal and Nemirovski (1999))
 Robustness with respect to constraints of a satisficing problem or an optimization problem.
- Robust Optimizing (eg. classical Maximin/Minimax) Robustness with respect to the objective function of an optimization problem.
- Robust Optimizing and Satisficing (eg. Ben-Tal and Nemirovski (2002))
 Robustness with respect to both the objective function and constraints of an optimization problem.

Robust I	Decision-Making	g			
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Classification

Robust Satisficing Problem $P(u), u \in U$: Find an $x \in X$ such that $q(x, \mathbf{u}) \in C$ Robust Optimizing Problem $P(u), u \in U$: $z^* := \operatorname{opt} f(x, \boldsymbol{u})$ $x \in X$ Robust Optimizing and Satisficing Problem $P(u), u \in U$: $z^* := \text{ opt } f(x, \mathbf{u})$ $x \in X(\mathbf{u})$

Degree of Robustness

- Complete (conventional)
 - $\forall u \in \mathcal{U}(x) \text{ (very conservative)}$
- Partial (eg. Starr (1962), Schneller and Sphicas (1983)) $\forall u \in U(x) \subseteq \mathcal{U}(x)$
- Local (eg. Ben-Haim (1996, 2001, 2006) $\forall u \in U(x, \tilde{u}) \subseteq \mathcal{U}(x)$ ($U(x, \tilde{u}) =$ neighborhood of \tilde{u})



Robust	Robust Decision-Making									
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Robustness á la MaximinComplete robustness $z^* := \max_{d \in \mathbb{D}} \min_{s \in S(d)} f(d, s)$ $= \max_{\substack{d \in \mathbb{D} \\ v \in \mathbb{R}}} \{v : f(d, s) \ge v, \forall s \in S(d)\}$

Maximin models for partial and local robustness are similar (a bit more complicated).

Voodooism

Info-Gap Conclusions

Voodoo Decision Theory



Encarta online Encyclopedia

Voodoo n

- A religion practiced throughout Caribbean countries, especially Haiti, that is a combination of Roman Catholic rituals and animistic beliefs of Dahomean enslaved laborers, involving magic communication with ancestors.
- Somebody who practices voodoo.
- A charm, spell, or fetish regarded by those who practice voodoo as having magical powers.
- A belief, theory, or method that lacks sufficient evidence or proof.



Voodoo	Decision The	eory			
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Decision Theory 000000000000

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Voodoo Decision Theory



Voodoo Decision Theory



Apparently very popular,

Example

The behavior of Kropotkin's cooperators is something like that of decision makers using Jeffrey expected utility model in the Max and Moritz situation. Are ground squirrels and vampires using voodoo decision theory?

> Brian Skyrms Evolution of the Social Contract Cambridge University Press, 1996.

Issue:

Evidential dependence, but causal independence.

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The legend

An old legend has it that an ancient treasure is hidden in an Asian-Pacific island.



You are in charge of the treasure hunt. How would you plan the operation?
Main issue: location, location!









1.2.3 Recipe

- Ignore the severity of the uncertainty.
- Socus on the substantially wrong estimate you have.
- Conduct the analysis in the immediate neighborhood of this estimate.

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Voodoo Decision-Making





Voodoo Decision-Making

Just in case, ..., the difficulty is that

Under severe uncertainty

The estimate we have is

- A wild guess.
- A poor indication of the true value.
- Likely to be substantially wrong.

Hence,

Beware!

Results obtained in the neighborhood of the estimate are likely to be substantially wrong in the neighborhood of the true value.





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$$\begin{array}{c} \text{Conventional Decision Theory} \\ GI \longrightarrow \mathfrak{Model} \longrightarrow GO \\ \text{Wrong} \longrightarrow \mathfrak{Model} \longrightarrow \text{Wrong} \end{array}$$

The robustness of any decision and the risk incurred in making that decision is only as good as the estimates on which it is based. Making estimation even more challenging, virtually all estimates that affect decisions are uncertain. Uncertainty can not be eliminated, but it can be managed.

Top Ten Challenges for Making Robust Decisions The Decision Expert Newsletter, Volume 1; Issue 2 http://www.robustdecisions.com/newsletter0102.php









What is the most popular Voodoo Decision Theory for robust decision-making under severe uncertainty in a number of research centers in

Australia



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Example

Predicting financial markets



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Applied ecology and conservation biology



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Impressive Self-Portrait

Voodooism

Info-Gap

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Info-gap decision theory is radically different from all current theories of decision under uncertainty. The difference originates in the modelling of uncertainty as an information gap rather than as a probability. The need for info-gap modeling and management of uncertainty arises in dealing with severe lack of information and highly unstructured uncertainty. Ben-Haim [2006, p. xii]

In this book we concentrate on the fairly new concept of information-gap uncertainty, whose differences from more classical approaches to uncertainty are real and deep. Ben-Haim [2006, p. 11]

Conclusions



Obvious Questions

- Does Info-Gap substantiate these very strong claims?
- Are these claims valid?

Not So Obvious Answers

- No, it does not.
- Ocertainly not.

It is therefore important to subject Info-Gap to a formal analysis – that actually should have been done seven years ago:

Info-Gap

FormalvsAnalysisClassical Decision Theory

Good news: should take no more than 5-10 minutes!

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Info-Gap)				

Meaning of Severe Uncertainty

- The region of uncertainty is usually relatively large, often unbounded.
- The uncertainty cannot be quantified by a probabilistic model.
- If there is an estimate of the parameter of interest, then the estimate is
 - A wild guess
 - A poor indication of the true value
 - Likely to be substantially wrong

Practical Meaning of Severe Uncertainty



bio-security homeland-security

Info-Gap Decision Theory

Decision Theory

Complete Generic Robustness Model

Voodooism

Info-Gap

$$\hat{\alpha}(r_c) := \max_{q \in \mathbb{Q}} \max \left\{ \alpha \ge 0 : r_c \le \min_{u \in \mathcal{U}(\alpha, \tilde{u})} R(q, u) \right\}$$
$$\mathcal{U}(\alpha, \tilde{u}) \subseteq \mathcal{U}(\alpha + \varepsilon, \tilde{u}), \forall \varepsilon > 0$$

Region of Severe Uncertainty, U



Conclusions

Complete Generic Robustness Model

$$\hat{\alpha}(r_c) := \max_{q \in \mathbb{Q}} \max \left\{ \alpha \ge 0 : r_c \le \min_{u \in \mathcal{U}(\alpha, \tilde{u})} R(q, u) \right\}$$

Fundamental FAQs

1	Is this new?	Definitely not!
2	Is this radically different?	Definitely not!
3	Does it make sense?	Definitely not!

So what is all this hype about Info-Gap ?!

Good question!

First Impression

Complete Generic Robustness Model

$$\hat{\alpha}(r_c) := \max_{q \in \mathbb{Q}} \max \left\{ \alpha \ge 0 : r_c \le \min_{u \in \mathcal{U}(\alpha, \tilde{u})} R(q, u) \right\}$$

Observations

- This model does not deal with severe uncertainty, it simply and unceremoniously ignores it.
- The analysis is invariant with \mathfrak{U} : the same solution for all \mathfrak{U} such that $\mathcal{U}(\hat{\alpha}(r_c), \tilde{u}) \subseteq \mathfrak{U}$.
- This model is fundamentally flawed.
- This model advocates voodoo decision-making.

First Impression

Fool-Proof Recipe

Step 1: Ignore the severe uncertainty.
Step 2: Focus instead on the poor estimate and its immediate neighborhood.

Region of Severe Uncertainty



Decision Theory Info-Gap Info-Gap Decision Theory First Impression Region of Severe Uncertainty



Recall that this is voodoo decision making!

Info-Gap Decision Theory

Complete Generic Robustness Model

$$\alpha^* := \max_{q \in \mathbb{Q}} \max \left\{ \alpha \ge 0 : r_c \le \min_{u \in \mathcal{U}(\alpha, \tilde{u})} R(q, u) \right\}$$

Fundamental Flaw



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More formally

Invariance Theorem (Sniedovich, 2007)

Info-Gap's robustness model is invariant to the size of the total region of uncertainty \mathfrak{U} for all \mathfrak{U} larger than $\mathcal{U}(\alpha^*, \tilde{u})$, where $\alpha^* := \hat{\alpha}(r_c)$. That is, the model yields the same results for all \mathfrak{U} such that

$$\mathcal{U}(\alpha^* + \varepsilon, \tilde{u}) \subseteq \mathfrak{U} \ , \ \varepsilon > o$$

Info-Gap Decision Theory

Info-Gap's Invariance Property



Maximin Theorem (Sniedovich 2007, 2008)

Info-Gap's robustness model is a simple instance of Wald's Maximin model. Specifically,

$$\begin{split} \alpha(q) &:= \max_{\alpha \ge 0} \left\{ \alpha : r_c \le \min_{u \in \mathcal{U}(\alpha, \tilde{u})} R(q, u) \right\} \ , \ q \in \mathbb{Q} \\ &= \max_{\alpha \ge 0} \min_{u \in \mathcal{U}(\alpha, \tilde{u})} \psi(q, \alpha, u) \end{split}$$

where

$$\psi(q, \alpha, u) := \begin{cases} \alpha , r_c \leq R(q, u) \\ 0 , r_c > R(q, u) \end{cases}, \alpha \geq 0, q \in \mathbb{Q}, u \in \mathcal{U}(\alpha, \tilde{u})$$

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Info-Gap: Typical misconception

Treasure Hunt



Myth:

How wrong can I be, yet be safe?

- Region of uncertainty.
- Estimate of the location.
 - Region affecting Info-Gap's analysis.
- True (unknown) location.

Fact:

Info-gap may conduct its robustness analysis in the vicinity of Brisbane (QLD), whereas for all we know the true location of the treasure may be somewhere in the middle of the Simpson desert or perhaps in down town Melbourne (VIC). Perhaps.



Australian Perspective



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Conclus	ions				

- Decision-making under severe uncertainty is difficult.
- It is a thriving area of research/practice.
- The Robust Optimization literature is extremely relevant.
- The Decision Theory literature is extremely relevant.
- The Operations Research literature is very relevant.
- Info-Gap's robustness model is neither new nor radically different.
- Info-Gap's uncertainty model is fundamentally flawed and is unsuitable for decision-making under severe uncertainty.
- Info-Gap Decision Theory exhibits a severe information-gap about the state of the art in decision-making under severe uncertainty.

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The Ten Natural Laws of Operations Analysis

- Ignore the problem and go immediately to the solution, that is where the profit lies.
- There are no small problems only small budgets.
- Names are control variables.
- Clarity of presentation leads to aptness of critique.
- Invention of the wheel is always on the direct path of a cost plus contract.
- **O** Undesirable results stem only from bad analysis.
- It is better to extend an error than to admit to a mistake.
- Progress is a function of the assumed reference system.
- Rigorous solutions to assumed problems are easier to sell than assumed solutions to rigorous problems.
- In desperation address the problem.

Bob Bedow, Interfaces 7(3), p. 122, 1979.

Conclusions Decision Theory Voodooism Info-Gap Black Swans, Modern Nostradamuses see The Spin Stops Here! Search me! Decision-Making Under Severe Fags | Help | @ | Contact | Uncertainty Logon time: Mon May 4 06:03:23 2009

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mighty maximin robust decisions responsible decisions

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FAQs?

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